



# Effects of the size and Cu modulation of Pd<sub>n</sub> (n ≤ 38) clusters on Hg<sup>0</sup> adsorption



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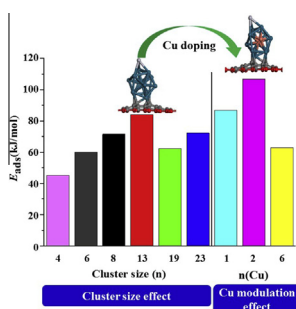
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## HIGHLIGHTS

- AC can enhance the stability of magic clusters Pd<sub>n</sub> (n = 4, 6, 8, 13, 19, 23).
- Pd<sub>n</sub> cluster size influences Hg<sup>0</sup> adsorption greatly, and Pd<sub>13</sub>/AC is optimal.
- CuPd<sub>12</sub>, Cu<sub>2</sub>Pd<sub>11</sub> and Cu<sub>6</sub>Pd<sub>7</sub> bimetallic clusters are relatively easy to obtain.
- The adsorption of Hg<sup>0</sup> is affected by Cu doping ratio, and Cu<sub>2</sub>Pd<sub>11</sub>/AC is the best.

## GRAPHICAL ABSTRACT



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## ABSTRACT

A density functional theory (DFT) method was used to study the adsorption of Hg<sup>0</sup> on activated carbon supported Pd<sub>n</sub> (n ≤ 38) clusters, the size and Cu modulation of Pd clusters were investigated. The adsorption energies of Hg<sup>0</sup> on Pd<sub>n</sub>/AC (n = 4, 6, 8, 13, 19, 23) show that the strongest adsorption strength is on the Pd<sub>13</sub>/AC. AC can prevent Pd clustering to a bulk and disperse cluster on the surface by comparing the interaction energy of Pd<sub>n</sub> cluster on AC with the binding energy per atom of corresponding Pd<sub>n</sub> cluster. Furthermore, some of Pd atoms in Pd<sub>13</sub> cluster were substituted by Cu atoms to improve the adsorption of Hg<sup>0</sup> and reduce the dosage of Pd. CuPd<sub>12</sub>, Cu<sub>2</sub>Pd<sub>11</sub> and Cu<sub>6</sub>Pd<sub>7</sub> are the most stable bimetallic clusters. In addition, the adsorption of Hg<sup>0</sup> shows that Cu<sub>2</sub>Pd<sub>11</sub>/AC is the most effective adsorbent for Hg<sup>0</sup>.

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## 1. Introduction

The removal of Hg<sup>0</sup> has caused wide public concerns and been studied by many researchers due to its low water solubility and chemical reactivity [1,2]. Different materials are adopted as sorbents for removing Hg<sup>0</sup>, including non-noble metal Cu [3], and metal oxides ZnO [4,5], CuO [6], V<sub>2</sub>O<sub>5</sub> [7] and Fe<sub>2</sub>O<sub>3</sub> [8]. However, the capture ability of Hg<sup>0</sup> is weak due to little adsorption energies

of Hg<sup>0</sup> on surfaces of these materials [4,5,9–11]. Therefore, Hg<sup>0</sup> is needed to be oxidized to oxides, followed by the removal of the oxidized mercury on account of a strong interaction between sorbents and oxidized mercury [12]. The above technical process is complex. It is known that noble metals, especially Pd, have high direct Hg<sup>0</sup> capture efficiency [13,14].

The adsorptions of Hg<sup>0</sup> on 22 pure metals were studied, and it was found that Pd is the most promising sorbent with the strongest Hg<sup>0</sup> adsorption capacity [15]. Also, the adsorption strength of Hg<sup>0</sup> on Ag, Au, Pt and Pd surfaces was an increased order, and the adsorption energies of Hg<sup>0</sup> on perfect and defected Pd(1 1 1) surface are 81.0 and 217.1 kJ·mol<sup>-1</sup>, respectively [16], higher than that

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on perfect and defected Au(1 1 1) surface with adsorption energies of 40.5 and 53.1 kJ·mol<sup>-1</sup>, respectively [17]. Nevertheless, the high price of Pd limits its wide application [18].

When the bulk size of noble metals was reduced to metal clusters containing only a few atoms, the loading amount of the noble metals can be largely reduced, as well as show unique chemical and physical properties [19,20]. Pd<sub>n</sub> clusters have been widely used in the treatment of automobile exhaust gas [21,22] for the high activity in heterogeneous catalytic reactions [23]. The catalytic activity of Pd<sub>n</sub> clusters is influenced greatly by the quantum size effect, and which can be improved by adjusting the size dimension, shown in the adsorptions of CO and NO, as well as the CO + NO reaction on Pd<sub>n</sub> clusters [23,24]. Similarly, adjusting the amount of loaded Pd on γ-Al<sub>2</sub>O<sub>3</sub> can enhance the removal efficiency of Hg<sup>0</sup> [16]. Therefore, obtaining the optimal size of Pd<sub>n</sub> cluster is very meaningful.

Graphene-based materials are as superior adsorbents for removing aromatic compounds from effluent [25], uranium from groundwater [26], and so on. In addition, the injection of graphite with 10% Pd resulted in a decrease of 98.2% of the total Hg concentration in a gas mixture consisting of ~11,000 ng/Nm<sup>3</sup> Hg, while injection of the single-walled carbon nanotubes (SWNT) with 10% Pd resulted in a decrease of 95.4% of the total Hg [27]. AC is one of graphene-based materials with large surface area and unique structure. The combination of AC and Pd may be an effective Hg<sup>0</sup> remover [28], in view of the high Hg<sup>0</sup> removal efficiency of Pd and specific surface of AC [29]. The removal efficiency of Hg<sup>0</sup> increased with the increasing of Pd loading amount on AC, but the effective utilization rate of loaded Pd decreased significantly simultaneously [14]. The removal efficiencies of Hg<sup>0</sup> are various with different supports. Thus, the effect of AC on the removal of Hg<sup>0</sup> is needed to be explored.

Additionally, the second metal doping can improve the catalytic activity of pure metals [30]. The alloying treatment of Pd<sub>n</sub> clusters increased the energy conversion rate of fuel cell [31,32]. Among all metals, Cu is one of non-noble metals, which is usually doped into the noble metal to reduce the cost of materials, as well as promote the stability and reactivity [33,34]. The addition of Cu into Pd/Al<sub>2</sub>O<sub>3</sub> and Pd/SiO<sub>2</sub> can enhance the stability of the catalyst [33]. Moreover, MPd<sub>12</sub> (M = Fe, Co, Ni, Cu, Zn) supported on the graphene with single vacancy (SV-G) show higher catalytic activity to the oxygen reduction reaction than that of Pd<sub>13</sub>/SV-G, in which CuPd<sub>12</sub> has the strongest interaction with the SV-G surface [34]. However, the effect of Cu modulation of Pd<sub>n</sub>/AC on the adsorption of Hg<sup>0</sup> is unclear.

In this work, the size effect of Pd<sub>n</sub> (n ≤ 38) clusters on Hg<sup>0</sup> adsorption will be studied. The magic clusters of Pd<sub>n</sub> (n ≤ 38) are obtained and are loaded on the AC. Then, the optimal size of loaded Pd<sub>n</sub> cluster is obtained by investigating adsorptions of Hg<sup>0</sup> on different Pd<sub>n</sub> clusters supported on the AC. Meanwhile, the effect of AC will be analyzed. Additionally, the optimal Pd<sub>n</sub> cluster will be modulated by Cu with different ratios to improve Hg<sup>0</sup> adsorption and reduce the dosage of Pd. The configurations and stability of different Cu-Pd bimetallic clusters are studied, and then, the adsorptions of Hg<sup>0</sup> on stable AC supported Cu-Pd bimetallic clusters are discussed to obtain the optimized Cu doping ratio.

## 2. Calculation method and model

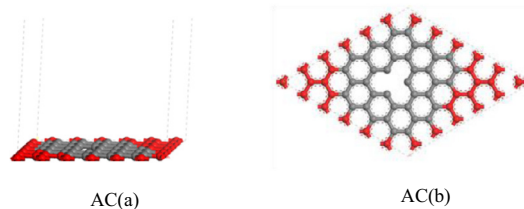
### 2.1. Computation method

All calculations were performed by the DMol<sup>3</sup> program package [35] in Materials Studio 5.5. The exchange and correlation energies were calculated using generalized gradient approximation (GGA) with Perdew-Wang exchange-correlation functional (PW91)

[36,37]. There are two main reasons for choosing the GGA-PW91 in the present work. Firstly, the binding energies of Pd atom on the single vacancy AC surface were calculated at PW91, Perdew-Burke-Ernzerhof (PBE) and Becke' hybrid exchange functional and the Lee-Yang-Parr (BLYP) functionals, which are 516.5, 506.7 and 441.2 kJ·mol<sup>-1</sup>. The similar results are obtained by PW91 and PBE functionals, which agree with the theoretical result of 518.1 kJ·mol<sup>-1</sup> by Ma et al. [38]. Secondly, PW91 function satisfies the known formal properties of the exact exchange-correlation functional [39], and which is widely used to study the structure and properties of Pd clusters [40–42]. Equivalent to 6-31G\*\* in Gaussian [43,44], the double numerical plus polarization (DNP) basis set [45] was employed for the valence electron functions. An all-electron basis set was applied to deal with carbon atoms, while relativistic effects were considered for Cu, Pd and Hg atoms with the inner electrons kept frozen and replaced by an effective core potentials (ECP) [46]. The Brillouin zone integrations within the Monkhorst Pack were 3 × 3 × 1 *k*-point according to the test and reported results [47,48]. A cutoff of 4.6 Å is chosen and a smearing of 0.005 Ha (1 Ha = 2625.5 kJ·mol<sup>-1</sup>) to the orbital occupation is applied to achieve accurate electronic convergence. For geometrical optimizations, the total energy, the maximum force and the maximum displacement were converged to 2 × 10<sup>-5</sup> Ha, 4 × 10<sup>-3</sup> Ha/Å and 0.005 Å, respectively. Spin polarization was performed considering that the carbon vacancies can induce magnetism by breaking the symmetry of the nonmagnetic perfect surface [49].

### 2.2. Surface model

As shown in our previous study [50], a single-layer p(6 × 6) graphite was taken to simulate AC surface by cleaving the optimized graphite structure with 71 carbon atoms, and a single carbon atom vacancy was on the surface [51,52]. The edge was fixed to minimize elastic interactions between periodic vacancy defects [51,53], as red spheres shown in Fig. 1. The Pd<sub>n</sub> clusters were constructed by adding one Pd atom to various possible binding sites of the preceding stable cluster. The structure was regarded as the most stable configuration with the lowest total energy and highest average binding energy in the isomers. As for the construction of Cu-Pd bimetallic clusters, one Pd atom in Pd<sub>13</sub> was substituted by Cu leading to CuPd<sub>12</sub>, and then another one was substituted from the preceding stable Cu-Pd bimetallic cluster leading to Cu<sub>m</sub>-Pd<sub>n-m</sub> (m = 2–6). The similar method was applied to obtain Cu<sub>m</sub>-Pd<sub>n-m</sub> (m = 12–7), in which one Cu atom in Cu<sub>13</sub> was substituted by a Pd forming Cu<sub>12</sub>Pd. Based on the reports [54,55], the site with the smallest substitution energy is preferred for the Cu substitution, and a bigger average binding energy corresponds to a higher stability. The average binding energy  $E_b(\text{Pd}_n)$ ,  $E_b(\text{Cu}_m\text{Pd}_{n-m})$  and substitution energy  $E_{\text{sub}}$  are defined as follows:



**Fig. 1.** The optimized slab model of the AC surface. (a) and (b) are the side view and top view of the AC surface, respectively. (The red and dark grey spheres represent the fixed and relaxation carbon atoms, respectively.). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

$$E_b(\text{Pd}_n) = [nE(\text{Pd}) - E(\text{Pd}_n)]/n \quad (1)$$

$$E_b(\text{Cu}_m\text{Pd}_{n-m}) = [mE(\text{Cu}) + (n-m)E(\text{Pd}) - E(\text{Cu}_m\text{Pd}_{n-m})]/n \quad (2)$$

$$E_{\text{sub}} = [E(\text{Cu}_m\text{Pd}_{n-m}) + mE(\text{Pd}) - E(\text{Pd}_n) - mE(\text{Cu})]/m \quad (3)$$

where  $E(\text{Pd})$  and  $E(\text{Cu})$  represent total electronic energies of Pd atom and Cu atom, respectively;  $E(\text{Pd}_n)$  and  $E(\text{Cu}_m\text{Pd}_{n-m})$  are total electronic energies of  $\text{Pd}_n$  clusters and Cu-Pd bimetallic clusters, respectively;  $n$  and  $m$  are numbers of Pd atoms and substituted Cu atoms;  $E_b(\text{Pd}_n)$  and  $E_b(\text{Cu}_m\text{Pd}_{n-m})$  are used to estimate the stability of  $\text{Pd}_n$  clusters and Cu-Pd bimetallic cluster; and  $E_{\text{sub}}$  reflects the substitution ability of Cu atom. A bigger value of  $E_b$  means a more stable  $\text{Pd}_n$  cluster and Cu-Pd bimetallic cluster, while a more negative value of  $E_{\text{sub}}$  implies an easier substitution of Cu atom [54,55].

### 3. Results and discussion

#### 3.1. $\text{Hg}^0$ adsorption on the Pd/AC surface

Firstly, the structure of AC loading a Pd atom (Pd/AC) and the adsorption of  $\text{Hg}^0$  on the Pd/AC surface are discussed. The result shows that the isolated Pd atom has a strong affinity to the C-defected site on the AC surface with an adsorption energy of  $516.5 \text{ kJ}\cdot\text{mol}^{-1}$ . In addition, there's a weak interaction between  $\text{Hg}^0$  and the Pd/AC surface, with a little adsorption energy of  $30.1 \text{ kJ}\cdot\text{mol}^{-1}$ , implying that Pd/AC is not an efficient mercury sorbent. Differently, Pd has been demonstrated that it has a high  $\text{Hg}^0$  removal efficiency in theory and experiment [14,56]. Steckel et al. [3] found that the order of the interaction strength between  $\text{Hg}^0$  and different metal surfaces is  $\text{Ag} < \text{Au} < \text{Cu} < \text{Ni} < \text{Pt} < \text{Pd}$ . And the adsorption energy of  $\text{Hg}^0$  on the defected Pd(111) surface is  $217.1 \text{ kJ}\cdot\text{mol}^{-1}$ , higher than that on the perfect surface with  $81.0 \text{ kJ}\cdot\text{mol}^{-1}$  [16]. The high  $\text{Hg}^0$  removal efficiency of metallic Pd has also been verified by the packed-bed reactor system, and the amount of  $\text{Hg}^0$  in simulated fuel gases was measured via the online atomic fluorescence spectrophotometer [57]. In addition, some clusters show stronger adsorption capacity than the surface. The adsorption energy of  $\text{H}_2$  on the Pd cluster is larger than that on the Pd surface [58], and similar cases for adsorptions of CO, H,  $\text{O}_2$  and O on the  $\text{Pt}_{55}$  cluster and Pt(111) surface [59]. It can be seen that proper clustering with a certain amount of atoms can improve the activity of metal greatly, and the aggregative state of Pd atoms will be studied to capture  $\text{Hg}^0$ .

#### 3.2. The evolution of $\text{Pd}_n$ ( $n = 2-8, 13, 19, 23, 38$ ) clusters and their stabilities

The stable configurations of  $\text{Pd}_n$  ( $n = 2-8$ ) clusters are obtained by calculations, which are made comparison with the literature report [41,42,60]. Therefore, the reliability of the calculation method and parameters adopted in the study will be verified. For the Pd clusters with the more Pd atoms (13, 19, 23 and 38), the stable configurations are obtained based on the results in literature [61–65].

##### 3.2.1. The evolution of $\text{Pd}_n$ ( $n = 2-8$ ) clusters

The possible structures and corresponding total energies for  $\text{Pd}_n$  ( $n = 2-8$ ) clusters are shown in Fig. S1 and Table S1 in the Supporting Information. In Fig. 2, we just show the most stable configurations of  $\text{Pd}_n$  ( $n = 2-8$ ) clusters. For  $\text{Pd}_2$  dimer, the linear structure is the only existent form with a bond length of  $2.560 \text{ \AA}$ , close to the reported values of  $2.565$  and  $2.555 \text{ \AA}$  [40,41]. When adding one Pd atom to the linear  $\text{Pd}_2$  cluster, we can obtain a triangular  $\text{Pd}_3$  cluster, with the average bond length of  $2.578 \text{ \AA}$ , in agreement with the reported value of  $2.589 \text{ \AA}$  [40]. Also, the bond angle ( $60^\circ$ ) is

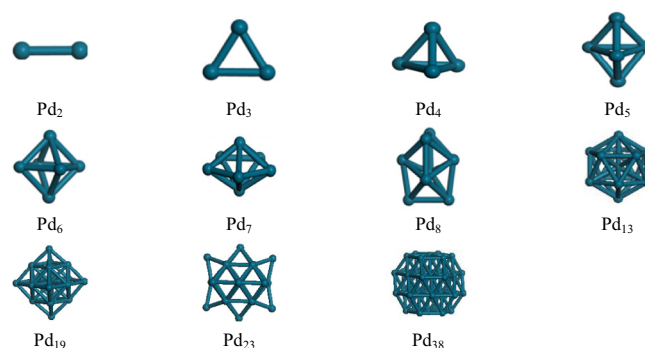


Fig. 2. The most stable configurations of  $\text{Pd}_n$  ( $n = 2-8, 13, 19, 23, 38$ ) clusters.

consistent with the result by Nava et al. [66]. The stable  $\text{Pd}_4$  cluster is tetrahedral, and the average bond length is  $2.661 \text{ \AA}$ , which is the same as the reported value [40]. For  $\text{Pd}_5$  cluster, the most stable configuration is trigonal bipyramid, with the average bond length of  $2.677 \text{ \AA}$  between the apex and equatorial atom, close to the reported value of  $2.660 \text{ \AA}$  [67]. Among the three isomers of  $\text{Pd}_6$  cluster, the octahedron  $\text{Pd}_6$  is the most stable configuration with the lowest energy, and the bond length between the apex and equatorial atom is  $2.702 \text{ \AA}$ , close to the reported value of  $2.690 \text{ \AA}$  [67]. There are two isomers for  $\text{Pd}_7$  cluster, and the pentagonal bipyramid  $\text{Pd}_7$  cluster is relatively more stable, with a bond length of  $2.727 \text{ \AA}$  from the apex to equatorial atom, also close to the reported value of  $2.760 \text{ \AA}$  [67]. For  $\text{Pd}_8$  cluster, three isomers are obtained, and the bicapped octahedral  $\text{Pd}_8$  cluster is the most stable configuration, the average bond length is  $2.706 \text{ \AA}$ , in agreement with the literature value of  $2.747 \text{ \AA}$  [68]. It can be seen that for a given  $\text{Pd}_n$  cluster, the isomer with a higher symmetry is more stable, in line with the literature reports [69].

##### 3.2.2. The stability of $\text{Pd}_n$ ( $n = 2-8, 13, 19, 23, 38$ ) clusters

The average binding energies ( $E_b$ ) per atom of  $\text{Pd}_n$  ( $n = 2-8$ ) clusters are calculated to investigate the stability. The relationship between  $E_b$  and the cluster size is shown in Fig. 3(a), in which the black line represents the variation trends of calculated values, while the red line is that of the literature values [41,60]. It can be seen that with the increase of  $\text{Pd}_n$  cluster size, the average binding energy increases monotonously, implying an enhancement of the stability of  $\text{Pd}_n$  ( $n = 2-8$ ) clusters. Besides, our calculated results give the same stability ranking for the Pd cluster as in the previous work [41], which confirms the rationality of the computational method and parameters further.

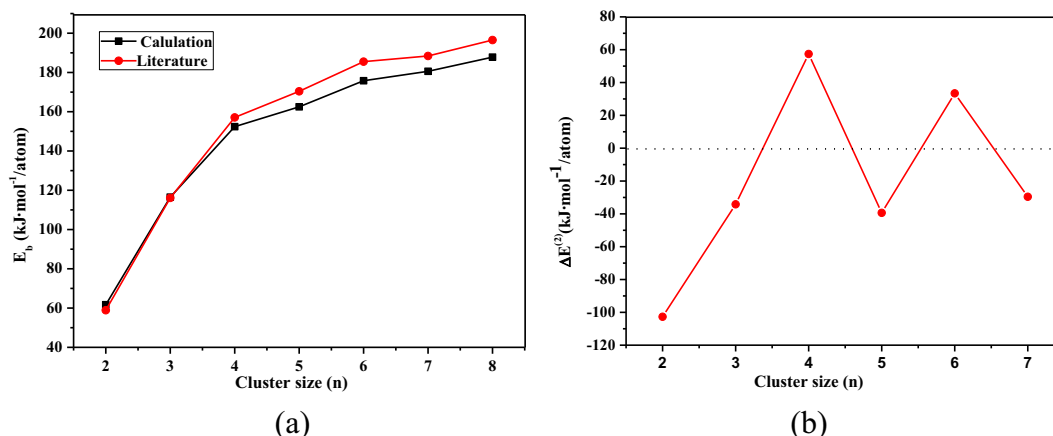
Magic clusters are species with particular stability, and are measured by mass spectroscopy in experiment [70]. To obtain the stable magic clusters with different sizes by theoretical method, the second energy difference  $\Delta_2E$  is calculated [61,63,71], which is defined as follows:

$$\Delta_2E = E(\text{Pd}_{n+1}) - 2E(\text{Pd}_n) + E(\text{Pd}_{n-1}) \quad (4)$$

$$\Delta E_0 = E(\text{Pd}_{n+1}) - E(\text{Pd}) - E(\text{Pd}_n) \quad (5)$$

$$\Delta E_1 = E(\text{Pd}_n) - E(\text{Pd}) - E(\text{Pd}_{n-1}) \quad (6)$$

where  $E(\text{Pd}_n)$ ,  $E(\text{Pd}_{n+1})$  and  $E(\text{Pd}_{n-1})$  represent energies of  $\text{Pd}_n$  cluster,  $\text{Pd}_{n+1}$  cluster and  $\text{Pd}_{n-1}$  cluster, respectively.  $\Delta_2E$  is the energy difference between  $\Delta E_0$  and  $\Delta E_1$  for fragmentation paths of  $\text{Pd}_{n+1} \rightarrow \text{Pd}_n + \text{Pd}$  and  $\text{Pd}_n \rightarrow \text{Pd}_{n-1} + \text{Pd}$ , and a positive value means an easier dissociation of  $\text{Pd}_{n+1}$  cluster than that of  $\text{Pd}_n$  cluster. The magic clusters are identified by comparing the  $\Delta_2E$ , which is more stable than its lighter and heavier neighbors and considered as a measure of the stability of the clusters [72].



**Fig. 3.** (a) The variation trend of the average binding energies with the cluster size; (b) the variation trend of the second energy differences with the cluster size. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

For  $Pd_n$  ( $n = 2-7$ ) clusters, the variation trends of  $\Delta_2E$  with the cluster size is shown in Fig. 3(b). It can be seen that the value of  $\Delta_2E$  show an odd-even alternation, and two peaks appear at  $n = 4$  and 6, indicating the special stability of  $Pd_4$  and  $Pd_6$  clusters. Simultaneously, it can be inferred that the  $Pd_8$  cluster is also a magic cluster and has been confirmed in the previous work [61,69].

In addition,  $Pd_{13}$ ,  $Pd_{19}$ ,  $Pd_{23}$  and  $Pd_{38}$  clusters are also magic clusters of  $Pd_n$  ( $n \leq 38$ ) as reported [61–65]. Their stable configurations are icosahedron, octahedron, polyicosahedron and truncated octahedron, respectively, as shown in Fig. 2. The average binding energies of  $Pd_{13}$ ,  $Pd_{19}$  and  $Pd_{23}$  are 214.0, 235.0 and 239.0 kJ·mol<sup>-1</sup>, respectively, agree with the reported values of 221.0, 238.0 and 244.5 kJ·mol<sup>-1</sup> [60]. For  $Pd_{38}$  cluster, the average binding energy increases to 259.6 kJ·mol<sup>-1</sup>, gradually approaches to the cohesive energy (375.3 kJ·mol<sup>-1</sup>/Pd) [63] of Pd bulk.

The magic clusters for  $Pd_n$  ( $n \leq 38$ ) are obtained according the above analysis, they are  $Pd_4$ ,  $Pd_6$ ,  $Pd_8$ ,  $Pd_{13}$ ,  $Pd_{19}$ ,  $Pd_{23}$  and  $Pd_{38}$ . In the following section, the interaction between these magic clusters and the AC surface will be studied to obtain the stable  $Pd_n$ /AC sorbents.

### 3.3. The interaction between the magic clusters $Pd_n$ ( $n \leq 38$ ) clusters and the AC surface

#### 3.3.1. The magic clusters $Pd_n$ ( $n \leq 38$ ) on the AC surface

The interaction between  $Pd_n$  clusters and the AC surface is discussed, and deformations of  $Pd_n$  clusters and AC are considered, similar to the case that the interaction between  $Au_{16}$  cluster and carbon defect site leads to structure distortions [73]. Thus, the interaction strength between  $Pd_n$  clusters and the AC surface is measured by the interaction energy  $E_{inter}$ , which is defined as follows:

$$E_{inter}(Pd_n/AC) = E_{ads}(Pd_n/AC) - E_{def}(AC) - E_{def}(Pd_n) \quad (7)$$

$$E_{ads}(Pd_n/AC) = E(Pd_n) + E(AC) - E(Pd_n/AC) \quad (8)$$

$$E_{def}(AC) = E'(AC) - E(AC) \quad (9)$$

$$E_{def}(Pd_n) = E'(Pd_n) - E(Pd_n) \quad (10)$$

where  $E_{ads}(Pd_n/AC)$  is the adsorption energy of  $Pd_n$  cluster on the AC, and  $E(Pd_n/AC)$  is the total electronic energy of AC supported  $Pd_n$  clusters in its equilibrium geometry;  $E(Pd_n)$  and  $E(AC)$  are total electronic energies of  $Pd_n$  cluster and AC before the interaction, while  $E'(Pd_n)$  and  $E'(AC)$  are values after the interaction;  $E_{def}(AC)$

and  $E_{def}(Pd_n)$  are deformation energies of AC and  $Pd_n$  cluster, respectively. A positive value of interaction energy corresponds to a strong interaction between  $Pd_n$  clusters and AC. The more positive is the value, the stronger is the interaction.

Various initial configurations are considered when these magic clusters are supported on the AC surface, including interactions between the top Pd atom, the Pd-Pd bridge and the Pd-Pd-Pd surface with the C-vacancy of AC. All possible configurations and energies are shown in Fig. S2 and Table S2 in the Supporting Information. Besides, the interaction energies, deformation energies and the ratio of deformation energies to the adsorption energy for different isomeric structures are compared, and the most configurations are obtained, as shown in Fig. 4. For  $Pd_4$  cluster, three optimized geometries  $Pd_4/AC(a-c)$  are obtained with one, two and three Pd atoms bonded to the dangling carbon at the C-vacancy site, respectively. AC has a bigger deformation than that of  $Pd_4$  cluster during the interaction between  $Pd_4$  cluster and AC. The deformation of AC in  $Pd_4/AC(a)$  is minimum, while in  $Pd_4/AC(c)$  is the maximum.  $Pd_4/AC(a)$  is the most stable configuration with the highest interaction energy of 428.9 kJ·mol<sup>-1</sup> for  $Pd_4/AC$ , as shown in Fig. 4. However,  $Pd_4/AC(b)$  is with the highest adsorption energy of 544.6 kJ·mol<sup>-1</sup>, so it was regarded as the stable structure by Jia et al. [40].

The most stable  $Pd_6/AC$ ,  $Pd_8/AC$ ,  $Pd_{13}/AC$ ,  $Pd_{19}/AC$ ,  $Pd_{23}/AC$  and  $Pd_{38}/AC$  are obtained when  $Pd_n$  clusters interact with the AC surface via the top Pd atom and the C-vacancy of AC site. It is worth mentioning that the optimized structure of  $Pd_{13}/AC$  is consistent with the previous work [74]. As listed in Table 1, AC has a bigger deformation than that of  $Pd_n$  ( $n = 6, 8, 13, 19, 23, 38$ ) clusters during the interaction processes. Additionally, it can be concluded that the AC supported  $Pd_n$  ( $n = 4, 6, 8, 13, 19, 23, 38$ ) clusters can stably exist for the strong interactions between  $Pd_n$  clusters and AC.

#### 3.3.2. The influence of AC on the stability of the magic clusters $Pd_n$ ( $n \leq 38$ )

The influence of AC on the stability of  $Pd_n$  ( $n = 4, 6, 8, 13, 19, 23, 38$ ) clusters is studied. It is measured by the average binding energy difference ( $\Delta E_b\%$ ) between bare  $Pd_n$  clusters ( $E_b$ ) and the AC supported  $Pd_n$  clusters ( $E'_b$ ), in which  $E_b$  can be calculated by Eq. (1);  $E'_b$  can be calculated by Eqs. (11) and (12); and  $\Delta E_b\%$  can be got by Eq. (13).

$$E = nE(Pd) + E(AC) - E(Pd_n/AC) \quad (11)$$

$$E'_b = (E - E_{inter})/n \quad (12)$$



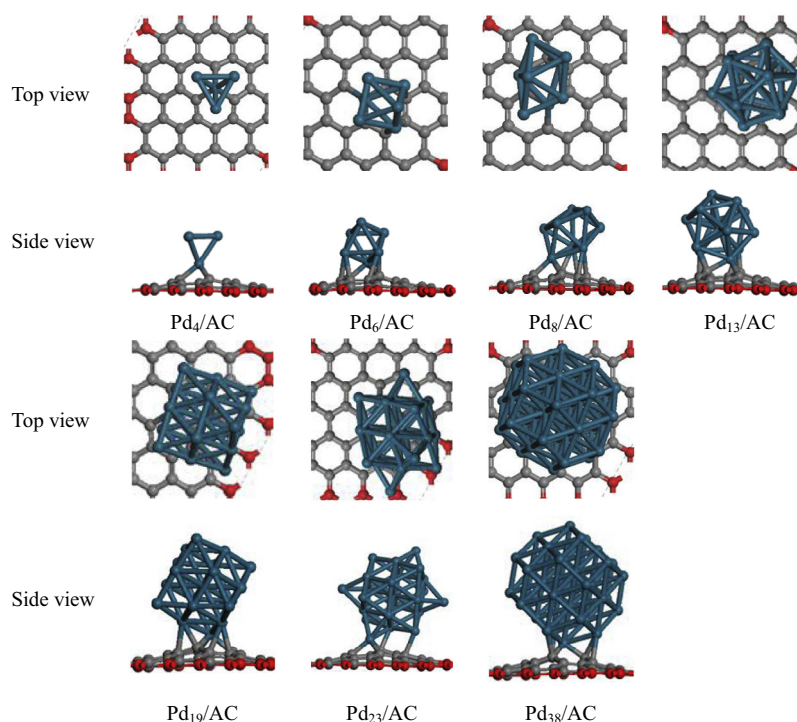


Fig. 4. The most stable configurations of magic clusters  $Pd_n$  ( $n \leq 38$ ) on the AC.

Table 1

The adsorption energies  $E_{ads}$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) and interaction energies  $E_{inter}$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) involved in the most stable configurations of AC supported magic clusters  $Pd_n$  ( $n \leq 38$ ),  $E_{def}$  (AC) and  $E_{def}$  ( $Pd_n$ ) ( $\text{kJ}\cdot\text{mol}^{-1}$ ) represent the deformation energies of AC surface and  $Pd_n$  clusters, while  $\Delta E_{def}$  (AC)% and  $\Delta E_{def}$  ( $Pd_n$ )% are the ratio of deformation energy to the adsorption energy, respectively.

Structure	$E_{ads}$	$E_{def}$ (AC)	$\Delta E_{def}$ (AC)%	$E_{def}$ ( $Pd_n$ )	$\Delta E_{def}$ ( $Pd_n$ )%	$E_{inter}$
$Pd_4$	526.9	97.0	18.4	1.1	0.2	428.9
$Pd_6$	580.9	140.4	24.2	0.9	0.2	439.6
$Pd_8$	594.0	144.6	24.4	6.0	1.0	443.3
$Pd_{13}$	628.8	187.3	29.8	21.2	3.4	420.3
$Pd_{19}$	532.5	142.5	26.8	13.6	2.5	376.5
$Pd_{23}$	546.4	141.2	25.8	12.7	2.3	392.5
$Pd_{38}$	596.4	201.3	33.8	10.6	1.8	384.6

$$\Delta E_b \% = [(E'_b - E_b)/E_b] \times 100\% \quad (13)$$

The  $E_b$  and  $E'_b$  for bare and AC supported  $Pd_n$  clusters are shown in Fig. 5(a). It can be seen that the average binding energies of both bare and AC supported  $Pd_n$  clusters increase monotonously with the increase of cluster size. In addition, the existence of AC can enhance the stability of  $Pd_n$  clusters for the higher average binding energies of  $Pd_n$  clusters on AC than bare cluster [75]. However, the enhancement decreases monotonously with the increase of cluster size, nearly no effect of AC on the stability of  $Pd_{38}$  cluster, as shown in Fig. 5(b). Therefore, only AC supported  $Pd_n$  ( $n = 4, 6, 8, 13, 19, 23$ ) clusters are considered to capture  $Hg^0$ .

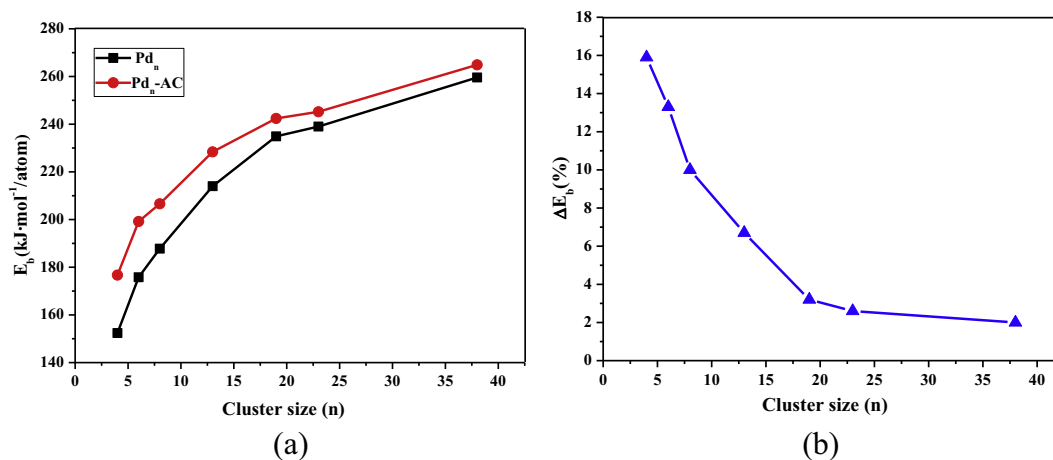
### 3.4. $Hg^0$ adsorption on $Pd_n/AC$ ( $n = 4, 6, 8, 13, 19, 23$ ) and $Pd_n$ cluster

For  $Hg^0$  adsorption on the  $Pd_n/AC$  ( $n = 4, 6, 8, 13, 19, 23$ ), three types of adsorption sites are taken into account, namely top (T), bridge (B) and hollow (H) sites, shown in Fig. 6. The most stable adsorption configurations are shown in Fig. 7, and the corresponding adsorption energies are shown in Fig. 8.

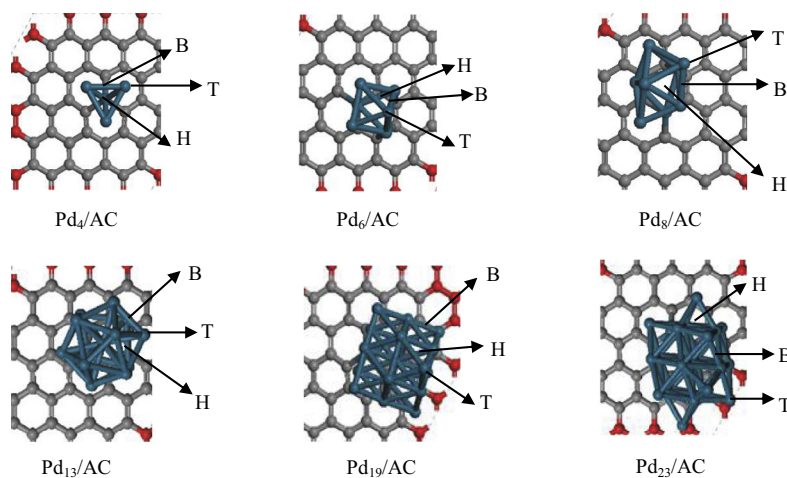
The stable adsorption structure for the interaction between  $Hg^0$  and  $Pd_4/AC$  is that  $Hg^0$  adsorbs on the top site of  $Pd_4/AC$ , with an

adsorption energy of  $45.3 \text{ kJ}\cdot\text{mol}^{-1}$ . Differently, in the most stable adsorption configurations of  $Hg-Pd_6/AC$ ,  $Hg-Pd_8/AC$  and  $Hg-Pd_{13}/AC$ ,  $Hg^0$  adsorbs stably on the bridge, hollow and hollow sites with adsorption energies of  $60.1$ ,  $71.6$  and  $84.0 \text{ kJ}\cdot\text{mol}^{-1}$ , respectively. The adsorption strength is in an increased order. In the most stable configurations of  $Hg-Pd_{19}/AC$  and  $Hg-Pd_{23}/AC$ ,  $Hg^0$  adsorbs on the hollow and bridge site, respectively. The adsorption energies are  $62.4$  and  $72.4 \text{ kJ}\cdot\text{mol}^{-1}$ , respectively.

To sum up, with the increase of the cluster size, the adsorption site of  $Hg^0$  on the most stable  $Pd_n/AC$  ( $n = 4, 6, 8, 13, 19$ ) configurations vary from top site to bridge site then to hollow site. But abnormality is for the  $Pd_{23}/AC$ , on which bridge site is the most favorable for  $Hg^0$  adsorption. The adsorption strength of  $Hg^0$  on the  $Pd_n/AC$  ( $n = 4, 6, 8, 13, 19, 23$ ) is in a zigzag-shape variation, as shown in Fig. 8. It can be concluded that loading the icosahedral  $Pd_{13}$  cluster on AC surface is relatively more favorable for  $Hg^0$  adsorption, in consistent with the finding that the easiest dissociation of  $H_2$  occurs on the  $Pd_{13}$  cluster among  $Pd_n$  ( $n = 4, 6, 13, 19, 55$ ) clusters [42]. Also, it has been found that the NO adsorption energy on icosahedral-based  $Pd_n$  clusters is higher than that on the octahedral configuration [68]. Recently, the adsorption of  $Hg^0$  on  $Pd/AC$  and  $Pd_{13}/AC$  has also been stud-



**Fig. 5.** (a) The average binding energy variation trends of the bare and AC supported Pd<sub>n</sub> ( $n = 4, 6, 8, 13, 19, 23, 38$ ) clusters, represented by the black and red lines, respectively; (b) the variation trend of the increased percentage  $\Delta E_b$ %. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 6.** The adsorption sites at the most stable Pd<sub>n</sub>/AC ( $n = 4, 6, 8, 13, 19, 23$ ) configurations.

ied, and it shows that the strength on Pd<sub>13</sub>/AC is higher than that Pd/AC [76].

In addition, we remove the AC support and calculate adsorption energies of Hg<sup>0</sup> on bare Pd<sub>n</sub> clusters for comparing and evaluating the effect of AC on clusters, the corresponding adsorption energies are shown in Fig. 8 (blue line). It can be seen that the energies are with little differences between Hg<sup>0</sup> on bare Pd clusters and Pd clusters with the same atoms supported on the AC. The largest difference occurs between Pd<sub>13</sub> and Pd<sub>13</sub>/AC with the energy of 11.3 kJ·mol<sup>-1</sup>. This shows AC cannot enhance the adsorption of Hg<sup>0</sup> on Pd cluster, but can promote more electrons to transfer from support to oxygen molecule and further make the O–O bond elongation [40]. Comparing the interaction energy of Pd<sub>n</sub> cluster on AC with the binding energy per atom of corresponding Pd<sub>n</sub> cluster, the former is higher than that of the latter one, which shows an attractive interaction between AC and Pd clusters, and AC can disperse cluster on the surface and prevent Pd clustering to a bulk [38].

### 3.5. The effect of Cu modulated Pd<sub>13</sub>/AC on Hg<sup>0</sup> adsorption

According to the above studies, it is known that the Pd<sub>13</sub>/AC shows an excellent Hg<sup>0</sup> adsorption among Pd<sub>n</sub>/AC ( $n = 4, 6, 8, 13, 19, 23$ ). In order to increase the Hg<sup>0</sup> capture capacity of Pd<sub>n</sub>/AC,

meanwhile reduce the dosage of Pd, the effect of Cu modulated Pd<sub>13</sub>/AC on Hg<sup>0</sup> adsorption is discussed in the following study.

#### 3.5.1. The configurations and stability of Cu<sub>n</sub>Pd<sub>13-n</sub> ( $n = 1-12$ ) bimetallic clusters

Configurations of Cu<sub>n</sub>Pd<sub>13-n</sub> ( $n = 1-12$ ) bimetallic clusters with different Cu atoms substituting Pd in the most stable Pd<sub>13</sub> cluster are investigated. All the possible structures and the corresponding substitution energies are shown in Fig. S3 and Table S3, respectively. The most stable configurations are shown in Fig. 9. For the CuPd<sub>12</sub> bimetallic cluster, the most stable configuration is that the central Pd atom of Pd<sub>13</sub> cluster is substituted by one Cu atom, which is similar to configurations of AuPd<sub>12</sub> and PdAu<sub>12</sub> clusters [77]. Next, one Cu atom substituting one surface Pd atom of CuPd<sub>12</sub> leads to the most stable Cu<sub>2</sub>Pd<sub>11</sub> configuration. For the Cu<sub>3</sub>Pd<sub>10</sub> cluster, three isomers are obtained and their substitution energies are similar, but the structure with three Cu atoms in the center axis of Pd<sub>13</sub> cluster is the most stable configuration for its high symmetry. The stable Cu–Pd clusters with 4–12 substituted Cu atoms are also obtained, as shown in Fig. 9.

The substitution energies of Cu<sub>n</sub>Pd<sub>13-n</sub> ( $n = 1-12$ ) bimetallic clusters are shown in Fig. 10. It can be seen that the substitution energies increase monotonously except at  $n = 6$  with the increase

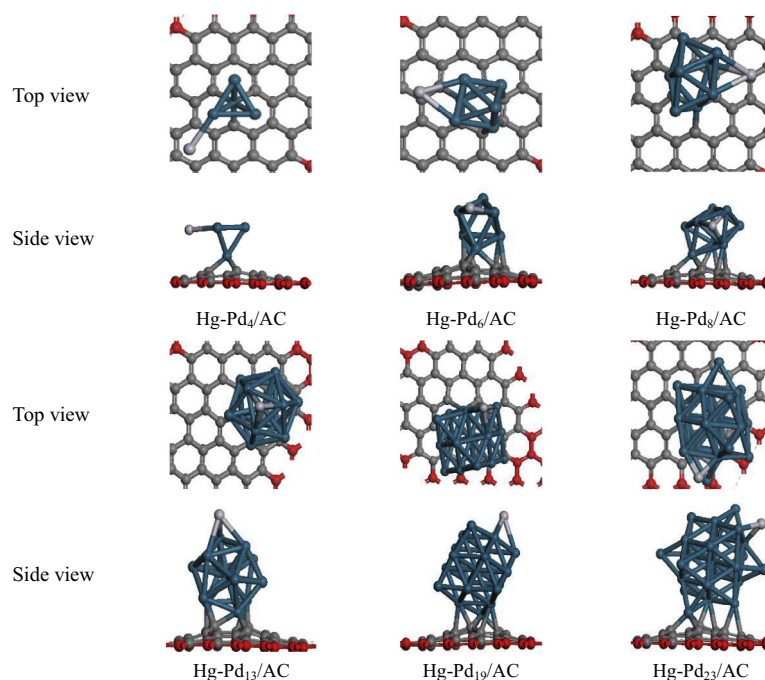


Fig. 7. The most stable adsorption configurations of  $\text{Hg}^0$  on  $\text{Pd}_n/\text{AC}$  ( $n = 4, 6, 8, 13, 19, 23$ ).

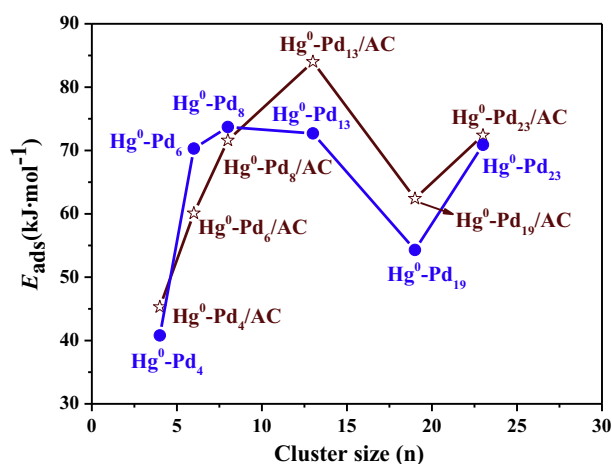


Fig. 8. The adsorption energies of  $\text{Hg}^0$  on the  $\text{Pd}_n/\text{AC}$  and naked  $\text{Pd}_n$  ( $n = 4, 6, 8, 13, 19, 23$ ) with the increase of cluster size. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

of substituted Cu atoms. When  $n = 9\text{--}12$  for the substituted Cu atoms, the values of substitution energies become positive, indicating that the maximum substitution number of Cu atom for  $\text{Pd}_{13}$  cluster is eight, namely the doping ratio is 61.5%. When one, two and six Pd atoms of  $\text{Pd}_{13}$  cluster are substituted by Cu atoms, the substitution energies are relatively more negative than others, meaning  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  clusters are formed easily.

The average binding energies of  $\text{Cu}_n\text{Pd}_{13-n}$  ( $n = 1\text{--}8$ ) bimetallic clusters listed in Table 2 are larger than that of  $\text{Pd}_{13}$  cluster with  $214.0 \text{ kJ}\cdot\text{mol}^{-1}$ , indicating that Cu doping can enhance the stability of  $\text{Pd}_{13}$  cluster. Combining the feasibility of Cu substitution and stability of the Cu-Pd bimetallic clusters,  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{-Pd}_7$  clusters are considered to be loaded on the AC surface.

### 3.5.2. The interactions between $\text{Cu}_n\text{Pd}_{13-n}/\text{AC}$ ( $n = 1, 2, 6$ ) and AC

The interactions between  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  bimetallic clusters and AC are discussed, which is necessary for the study

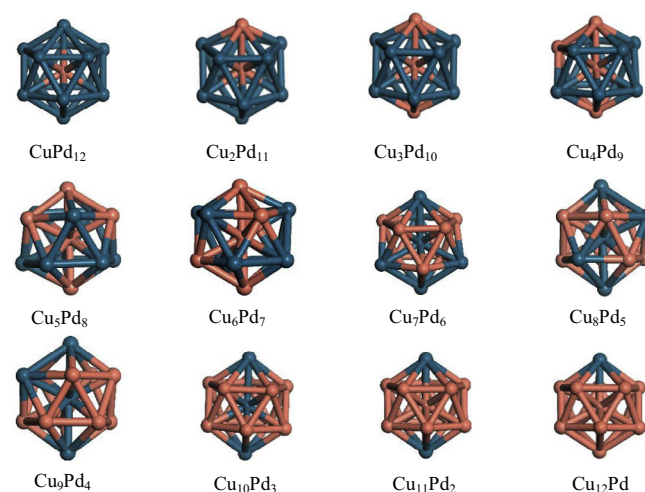


Fig. 9. The most stable configurations of  $\text{Cu}_n\text{Pd}_{13-n}$  ( $n = 1\text{--}12$ ) bimetallic clusters.

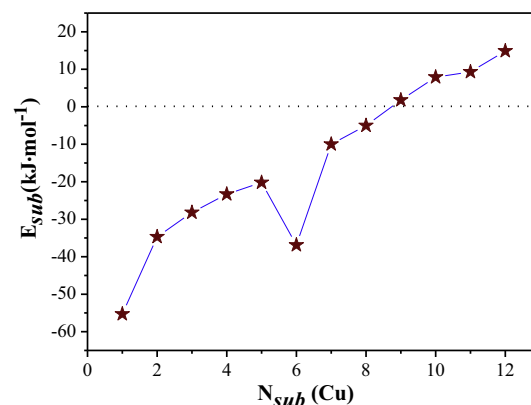


Fig. 10. The variation trends of the substitution energies of  $\text{Cu}_n\text{Pd}_{13-n}$  ( $n = 1\text{--}12$ ) bimetallic clusters with the substituted Cu atoms.

**Table 2**The average binding energies  $E_b$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) of  $\text{Cu}_n\text{Pd}_{13-n}$  ( $n = 1-8$ ) bimetallic clusters.

Clusters	$E_b$	Clusters	$E_b$
$\text{CuPd}_{12}$	218.2	$\text{Cu}_5\text{Pd}_8$	221.7
$\text{Cu}_2\text{Pd}_{11}$	219.3	$\text{Cu}_6\text{Pd}_7$	231.0
$\text{Cu}_3\text{Pd}_{10}$	220.5	$\text{Cu}_7\text{Pd}_6$	219.3
$\text{Cu}_4\text{Pd}_9$	221.1	$\text{Cu}_8\text{Pd}_5$	217.1

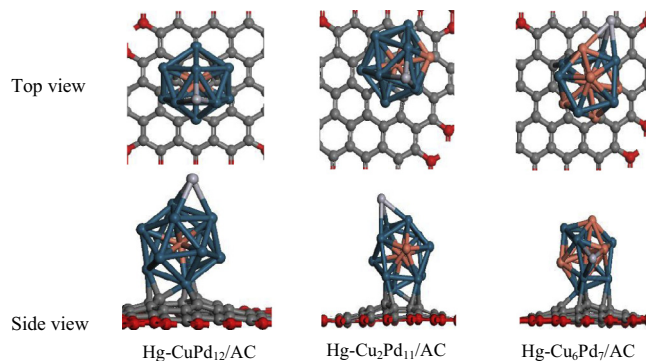
of  $\text{Hg}^0$  adsorption on the AC supported Cu-Pd bimetallic cluster. Similar to the interaction between  $\text{Pd}_{13}$  cluster and AC, two initial modes are considered, namely the top of each atom and the facet of three atoms interact with the AC, respectively. All possible configurations are shown in Figs. S4–S6, and relative energies are listed in Tables S4–S6. In addition, the interaction energies between AC and Cu-Pd bimetallic clusters are calculated to obtain the most stable AC supported Cu-Pd bimetallic clusters, which are shown in Fig. 11, and Table 3 lists the relative energies.

There are two, five and thirteen configurations for  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  bimetallic clusters interacting with AC, respectively, shown in  $\text{CuPd}_{12}/\text{AC}$  (a–b),  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  (a ~ e) and  $\text{Cu}_6\text{Pd}_7/\text{AC}$  (a–m) in Figs. S4–S6. By the comparison of their interaction energies shown in Tables S4–S6, the most stable configurations of  $\text{CuPd}_{12}/\text{AC}$ ,  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  and  $\text{Cu}_6\text{Pd}_7/\text{AC}$  are obtained. It can be seen that Pd atoms bound to the C atoms at the vacancy of AC surface, indicating that there is a strong interaction between Pd atom and  $sp^2$  dangling bonds of these three C atoms, in consistent with other studies [34,74]. From Table 3, it can be seen that AC has a bigger deformation than that of  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  clusters. Besides, the large interaction energies indicates that  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  bimetallic clusters can stably exist on the AC surface.

### 3.5.3. $\text{Hg}^0$ adsorption on $\text{Cu}_n\text{Pd}_{13-n}/\text{AC}$ ( $n = 1, 2, 6$ )

For  $\text{Hg}^0$  adsorption on the  $\text{CuPd}_{12}/\text{AC}$ ,  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  and  $\text{Cu}_6\text{Pd}_7/\text{AC}$ , three types of adsorption sites including top, bridge and hollow sites are considered. The most stable adsorption configurations and corresponding adsorption energies are shown in Fig. 12 and Table 4.

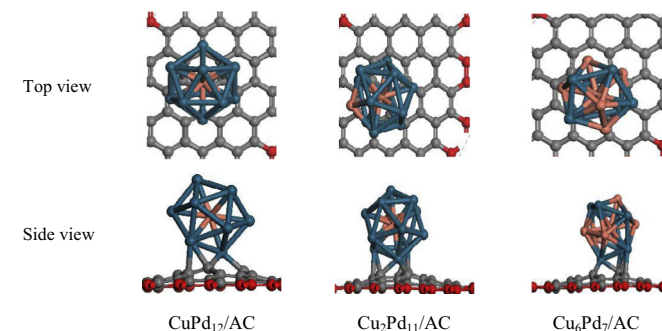
$\text{Hg}^0$  can stably adsorb on the hollow site of  $\text{CuPd}_{12}/\text{AC}$  and  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  formed by three Pd atoms, and the adsorption energies are 86.8 and 106.8  $\text{kJ}\cdot\text{mol}^{-1}$ , respectively. Hg-Pd bond lengths are

**Fig. 12.** The most stable configurations of  $\text{Hg}^0$  on the  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$ ,  $\text{Cu}_6\text{Pd}_7/\text{AC}$  and  $\text{CuPd}_{12}/\text{AC}$ , including the top and side views.**Table 4**The adsorption energies  $E_{\text{ads}}$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) of  $\text{Hg}^0$  on the most stable  $\text{CuPd}_{12}/\text{AC}$ ,  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  and  $\text{Cu}_6\text{Pd}_7/\text{AC}$  surface.

Configuration	$E_{\text{ads}}$
$\text{Hg-CuPd}_{12}/\text{AC}$	86.8
$\text{Hg-Cu}_2\text{Pd}_{11}/\text{AC}$	106.8
$\text{Hg-Cu}_6\text{Pd}_7/\text{AC}$	62.9

2.815, 2.873 and 2.888 Å for  $\text{Hg}^0$  interacting with  $\text{CuPd}_{12}/\text{AC}$ , and 2.843, 2.859 and 2.918 Å for  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$ , respectively. On the  $\text{Cu}_6\text{Pd}_7/\text{AC}$ ,  $\text{Hg}^0$  adsorbs on the hollow site formed by one Cu atom and two Pd atoms, and the bond length of Hg-Cu is 2.991 Å, while the two Hg-Pd bonds are 2.874 and 2.896 Å, respectively. The adsorption energy is 62.9  $\text{kJ}\cdot\text{mol}^{-1}$ . Comparing with the adsorption energy of  $\text{Hg}^0$  on  $\text{Pd}_{13}/\text{AC}$ , which increases by 3.3% when the doping ratio of Cu is 7.7%. It can be seen that only a slight improvement occurs for  $\text{Hg}^0$  adsorption on  $\text{CuPd}_{12}/\text{AC}$ . For  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$ , the adsorption energy increases greatly by 27.1% and the doping ratio of Cu is 15.4%, which is in favor of  $\text{Hg}^0$  adsorption. However, when the number of substituted Cu atoms increases to six and the doping ratio reaches up to 46.2%, the adsorption energy decreases by 25.1%, which is unfavorable for  $\text{Hg}^0$  adsorption. The results are well consistent with the previous result [78] that a mole fraction of Cu with 12.5–25% in Cu-Pd alloy can well promote  $\text{Hg}^0$  adsorption, but an inhibiting effect produces when the mole fraction is more than 25%. Meanwhile, we can see that  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  is the optimal bimetal adsorbent for  $\text{Hg}^0$ .

In addition, electronic properties including Mulliken charges and partial density of states (PDOS) for  $\text{Hg}^0$  adsorption on  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  are studied. 0.078  $e$  transfers from Hg to  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$ , which is higher than that on  $\text{Pd}_{13}/\text{AC}$  with 0.065  $e$ , meaning that  $\text{Hg}^0$  has a stronger interaction on  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  comparing with  $\text{Pd}_{13}/\text{AC}$ . In addition, during the interaction between  $\text{Hg}^0$  and  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$ , the PDOS for Hg-Pd bonding is analyzed, shown in Fig. 13(a–b). After the isolated Hg atom interacting with the  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  surface, all the states of Hg atom shift down, the  $s$ ,  $p$  states broadened and

**Fig. 11.** The most stable configurations of  $\text{CuPd}_{12}/\text{AC}$ ,  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  and  $\text{Cu}_6\text{Pd}_7/\text{AC}$ .**Table 3**The adsorption energies  $E_{\text{ads}}$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) and interaction energies  $E_{\text{inter}}$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) involved in the most stable AC supported  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  bimetallic clusters.  $E_{\text{def}}$  (AC) and  $E_{\text{der}}$  (cluster) ( $\text{kJ}\cdot\text{mol}^{-1}$ ) represent the deformation energies of AC surface and Cu-Pd bimetallic clusters, while  $\Delta E_{\text{def}}$  (AC)% and  $\Delta E_{\text{der}}$  (cluster)% are rates of the deformation energies, respectively.

Configuration	$E_{\text{ads}}$	$E_{\text{der}}$ (AC)	$\Delta E_{\text{der}}$ (AC)%	$E_{\text{der}}$ (cluster)	$\Delta E_{\text{der}}$ (cluster)%	$E_{\text{inter}}$
$\text{CuPd}_{12}/\text{AC}$	586.5	162.7	27.7%	12.8	2.2%	411.0
$\text{Cu}_2\text{Pd}_{11}/\text{AC}$	576.9	152.6	26.5%	7.1	1.2%	417.2
$\text{Cu}_6\text{Pd}_7/\text{AC}$	409.6	137.1	33.5%	124.9	30.5%	147.6



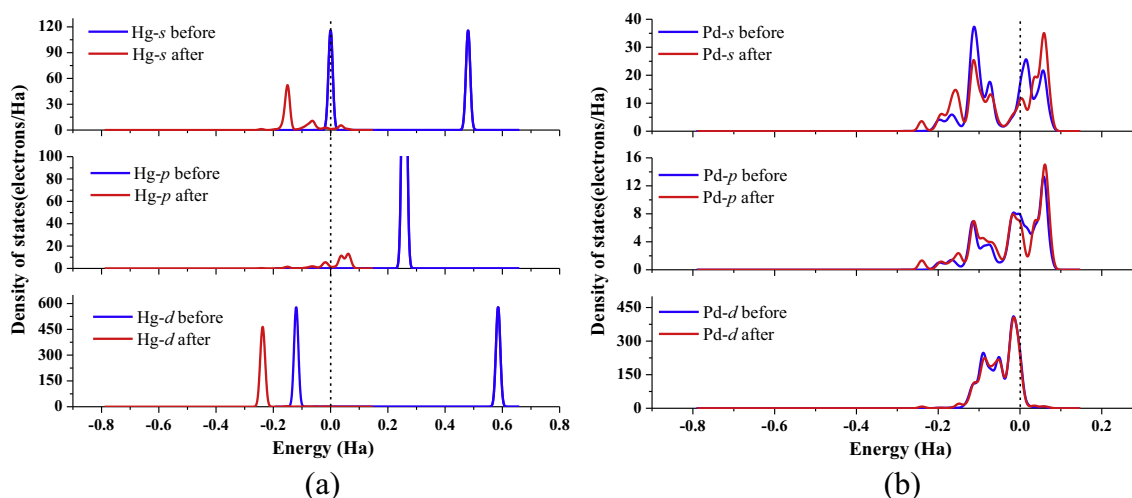


Fig. 13. The PDOS of Hg and Pd before and after interacting.

the electron density significantly reduced, implying a strong interaction between  $\text{Hg}^0$  and the  $\text{Cu}_2\text{Pd}_{11}/\text{AC}$  surface. Differently, there's almost no change for the  $d$  state of Pd. It can be concluded that the  $d$  state of Pd nearly has no effect on the bonding, similar to the case of  $\text{Hg}^0$  adsorption on the  $\text{CuO}(1\ 1\ 0)$  [79]. Based on the information contained after adsorption, there are overlaps between the  $s$  and  $p$  states of Hg and  $p$  state of Pd at approximately  $-0.15$  and  $0.07$  Ha, demonstrating the bonding mechanism.

#### 4. Conclusion

The size and Cu modulation effects on  $\text{Hg}^0$  adsorption have been clarified by the density functional theory (DFT) method. For the size effect, activated carbon supported  $\text{Pd}_n$  ( $n \leq 38$ ) clusters are used for  $\text{Hg}^0$  adsorption. It shows that the interaction energy of  $\text{Pd}_n$  cluster on AC is higher than the binding energy per atom of corresponding  $\text{Pd}_n$  cluster, which shows AC can disperse cluster on the surface and prevent Pd clustering to a bulk. The adsorption strength of  $\text{Hg}^0$  on  $\text{Pd}_n/\text{AC}$  ( $n = 4, 6, 8, 13, 19, 23$ ) shows a zigzag-shape variation, and when loading the icosahedral  $\text{Pd}_{13}$  cluster on AC, the adsorption of  $\text{Hg}^0$  is the strongest, with an adsorption energy of  $84.0\text{ kJ}\cdot\text{mol}^{-1}$ .

For the Cu modulation effect, the substitution of  $\text{Pd}_{13}$  cluster by 1–12 Cu atoms is studied, showing that  $\text{Pd}_{13}$  cluster can be substituted by eight Cu atoms at most and the  $\text{Cu}_n\text{Pd}_{13-n}$  ( $n = 1-8$ ) bimetallic clusters have a higher stability than that of  $\text{Pd}_{13}$  cluster. Besides, substituting one, two and six Pd atoms of  $\text{Pd}_{13}$  cluster by Cu atoms are relatively easy, and  $\text{CuPd}_{12}$ ,  $\text{Cu}_2\text{Pd}_{11}$  and  $\text{Cu}_6\text{Pd}_7$  bimetallic clusters can exist stably on the AC. As for the adsorption of  $\text{Hg}^0$  on Cu-modulated  $\text{Pd}_{13}$  clusters, the doping ratios of Cu affect the adsorption greatly. Substituting the center Pd atom of  $\text{Pd}_{13}$  cluster by Cu atom has a slight improvement for  $\text{Hg}^0$  adsorption, while increasing the number of substituted Cu atoms to two can improve the adsorption energy of  $\text{Hg}^0$  to  $106.8\text{ kJ}\cdot\text{mol}^{-1}$ , in favor of  $\text{Hg}^0$  adsorption. However, when the number of substituted Cu atoms increases to six, the adsorption energy decreases to  $62.9\text{ kJ}\cdot\text{mol}^{-1}$ , unfavorable for  $\text{Hg}^0$  adsorption.

#### Acknowledgments

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#### Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.cej.2016.09.004>.

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